

Stéphane Gonzalez

## Evaluation 1

Let  $A$ ,  $B$  and  $C$  be three sets, and  $p$ ,  $q$  and  $r$  be three propositions. For each of the following statements, say if it is **TRUE** or **FALSE**. (+1 if your answer is correct, -1 if your answer is wrong, 0 otherwise.)

1. The power set  $2^A$  of a set  $A$  is never empty. **TRUE**
2.  $A \cap B = \emptyset \Rightarrow A \neq B$ . **FALSE** (EX:  $A = B = \emptyset$ )
3. If  $f : A \rightarrow B$ , then  $f(A) = B$ . **FALSE** (EX:  $A = B = \{a, b, c\}$  and  $f(a) = f(b) = f(c) = a$ ).
4. If  $f : A \rightarrow B$ , then  $f^{-1}(B) = A$ . **TRUE**
5.  $[(A \subseteq B) \wedge (B = f(A))] \Rightarrow A = f^{-1}(B)$ . **FALSE** (EX:  $f(x) = |x|$ ,  $\forall x \in \mathbb{R}$  and  $A = B = [0, 1]$ ,  $f^{-1}(B) = [-1, 1] \neq A$ .)
6.  $[\neg((p \vee q) \rightarrow r)] \leftrightarrow [\neg(p \vee q) \rightarrow \neg r]$ . **FALSE**
7.  $((p \wedge \neg p) \vee (q \wedge (\neg q))) \rightarrow r$ . **TRUE**
8.  $\{1\} \in \{\{1, 2\}\}$ . **FALSE**
9.  $\emptyset \in 2^A$ . **TRUE**
10.  $\emptyset \subseteq 2^A$ . **TRUE**
11.  $\emptyset \subseteq (A \cap B)$ . **TRUE**
12.  $\{1, 2\} \in \{1, 2\}$  **FALSE**
13.  $\bigcap_{C \in \{\emptyset, \{1, 2\}, \{1\}\}} C = \{1\}$ . **FALSE**
14.  $\bigcup_{C \in \{\emptyset, \{1, 2\}, \{1\}\}} C = \{1, 2\}$ . **TRUE**
15. "If it is raining then the world has a beginning or the world has an end" if and only if "it is not raining or the world has a beginning or the world has an end." **TRUE**
16. The negation of "If it is raining then the world has a beginning or the world has an end" is "It is raining and the world has not beginning nor end." **TRUE**
17.  $A \cap (B \cup C) = (A \cup B) \cap (A \cup C)$ . **FALSE** (EX:  $A = \emptyset$  and  $B = C \neq \emptyset$ ).

18.  $(x \in A) \wedge (x \in B) \wedge (x \notin A \cup B)$ .FALSE
19.  $(\forall A)(\forall B)((x \in A) \vee (x \in B)) \Rightarrow (x \in A \cap B)$ .FALSE
20.  $[(x \in A \setminus B) \vee (x \in B \setminus C)] \wedge [(x \in B \setminus A) \wedge (x \in C \setminus B)]$ .FALSE